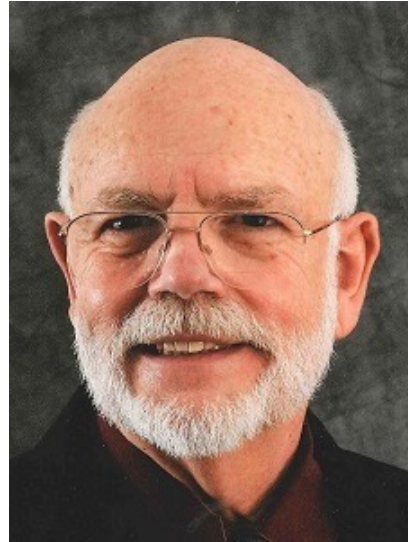


From Fully Differential Electron to Ion Impact Studies of Ionization: the Legacy of Don Madison

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Most important goal of atomic collision research: study quantum-mechanical few-body problem, one of the most fundamentally important and yet unsolved problems in physics

Essence of FBP: Schrödinger equation not analytically solvable for more than two mutually interacting particles even if forces are precisely known.

Particularly challenging: dynamic few-body systems like e.g. fragmentation processes.

Atomic fragmentation particularly suitable because:

- underlying interaction (electromagnetic) understood**
- can select systems with small particle number ($\approx 3 - 5$)**

Kinematically complete experiments

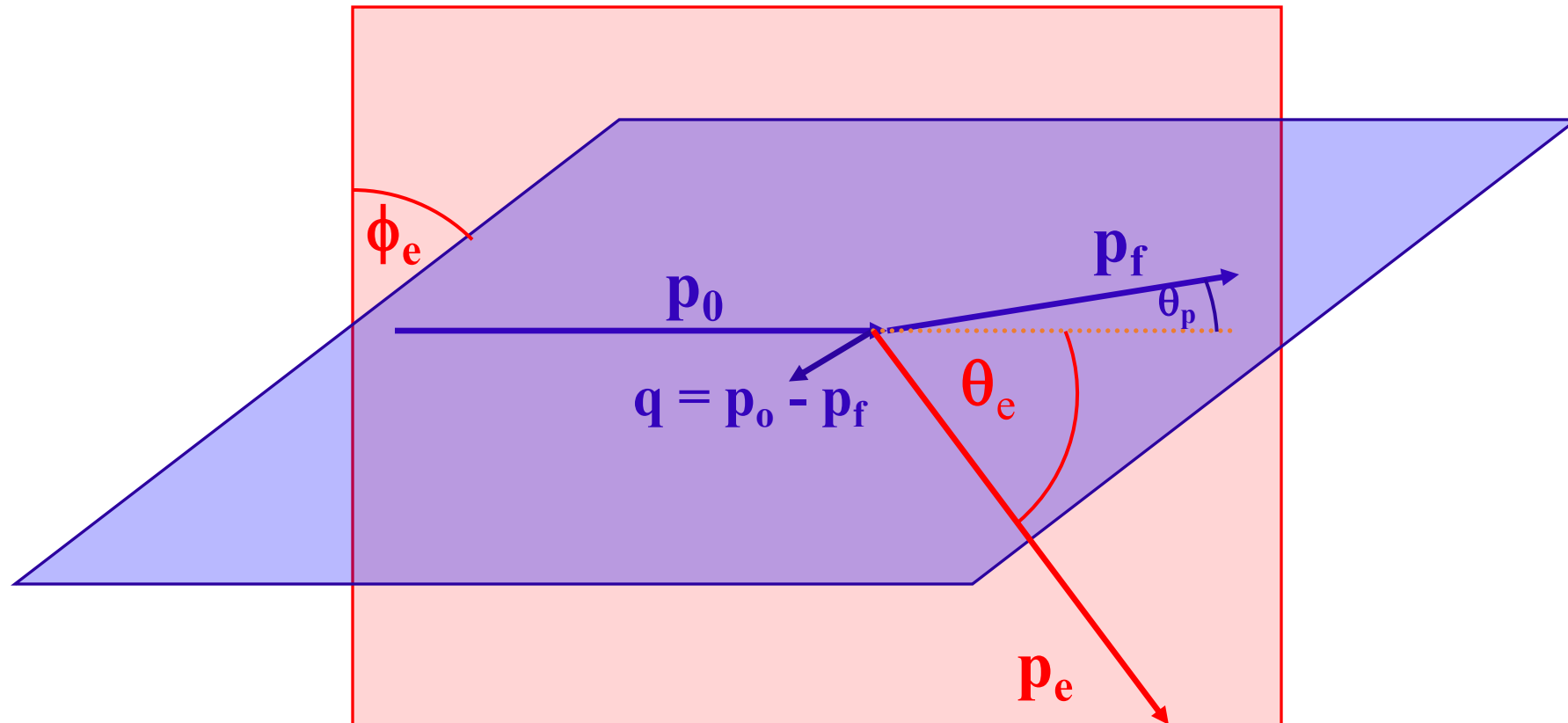
Where Don had to work on me (really hard and persistently): how to present results of a kinematically complete experiment on ionization

Typical e,2e experiment:
energy and angles of both final-state electrons measured **in coincidence**
⇒ FDCS usually presented as angular distribution of ejected electrons with all other parameters fixed.

Typical ion-impact experiment:
Earlier, either projectile scattering angle or electron spectra measured, but **not in coincidence**. With advent of **COLTRIMS**, electrons or projectiles measured **in coincidence with recoil ions**. ⇒ Usually, momentum distribution of various particles presented.

Advantage of fully differential electron angular distribution: more transparent
Often, structures in FDCS directly reflect interactions underlying reaction dynamics

Collision geometry and coordinate system

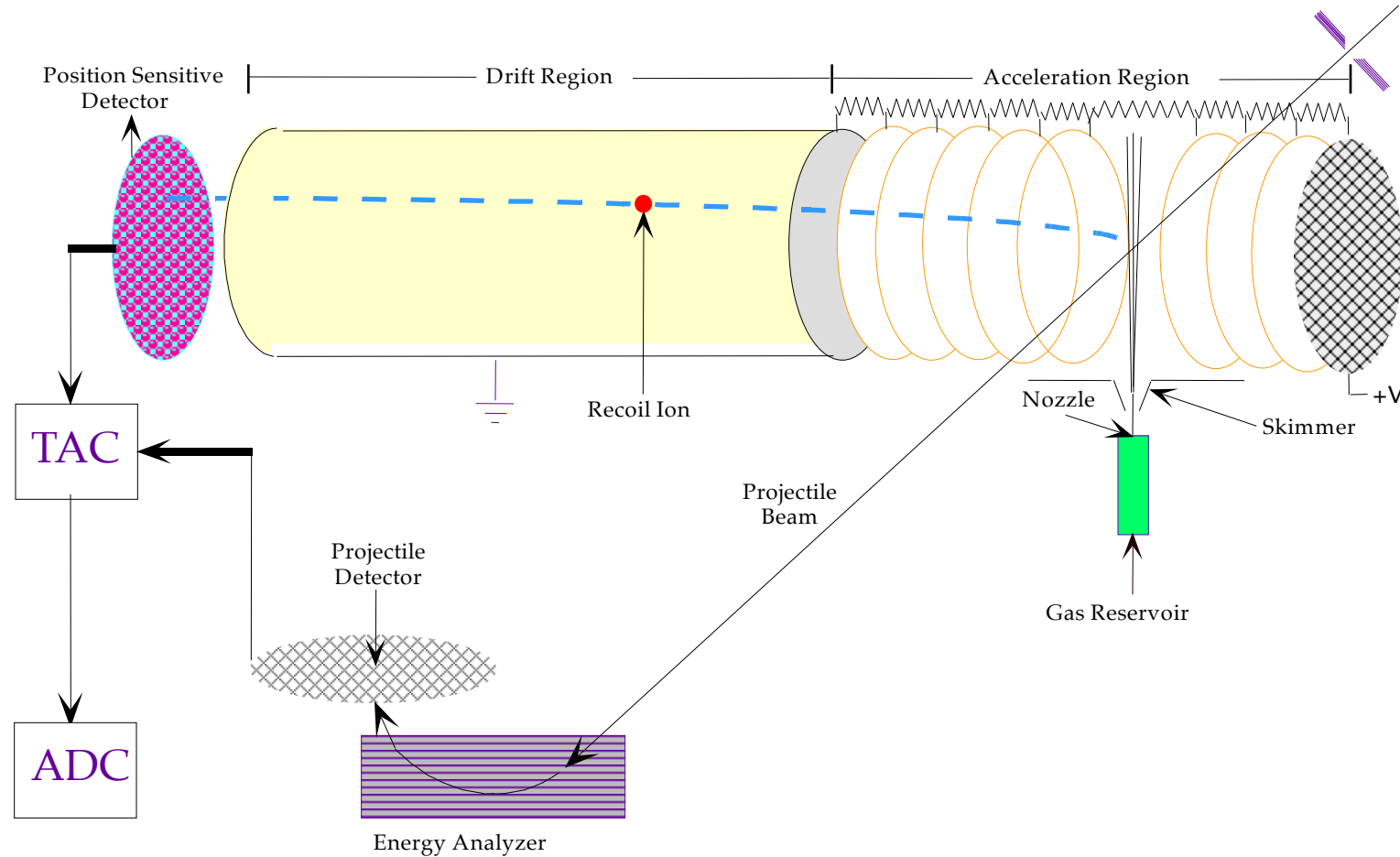


Blue: Scattering plane
defined by \mathbf{p}_0 and \mathbf{p}_f

Red: electron emission plane
defined by \mathbf{p}_0 and \mathbf{p}_e

Quantities fixed: $\phi_p = 0$, θ_p , $\phi_e = 0$, and \mathbf{E}_e , spectra plotted as a fct. of θ_e

Experimental Setup, 75 keV p + He



Complete projectile and recoil-ion momenta measured. Electron momentum from conservation laws \Rightarrow kinematically complete \Rightarrow FDCS

Ionization of simple atoms or molecules by ion impact

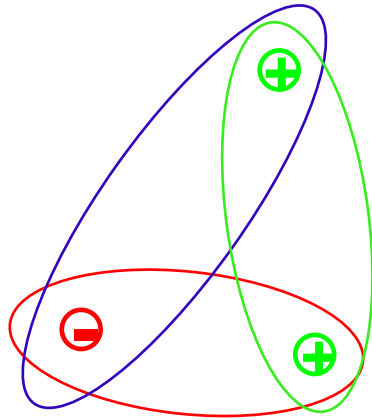
Perturbative treatment: Born series

$$T = \langle e^{ik_f r} \varphi_f | V | e^{ik_i r} \varphi_i \rangle + \langle e^{ik_f r} \varphi_f | V G_0 V | e^{ik_i r} \varphi_i \rangle + \\ \langle e^{ik_f r} \varphi_f | V G_0 V G_0 V | e^{ik_i r} \varphi_i \rangle + \dots$$

Distorted wave methods

Higher-order contributions treated in wavefunction of system

Break up three-body system into **3 two-body systems**:



Continuum eigenstate of each two-body subsystem is a **Coulomb-wave**.

Approximation: Represent total wavefunction as product of three Coulomb terms

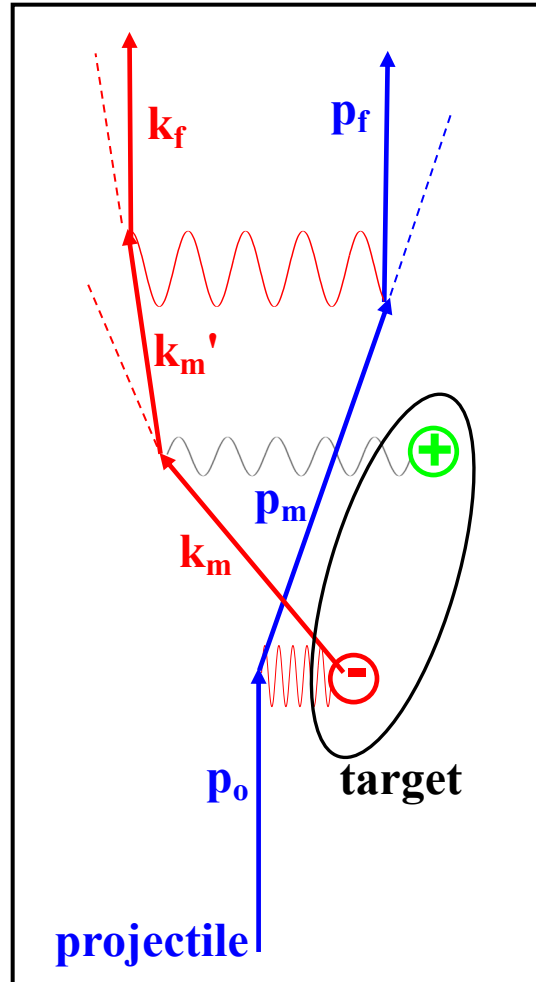
$$\Psi_f = C_{Pe} C_{PT} C_{Te}$$

3C wavefunction ignores correlations between particle pairs \Rightarrow
only accurate if one particle far from other two

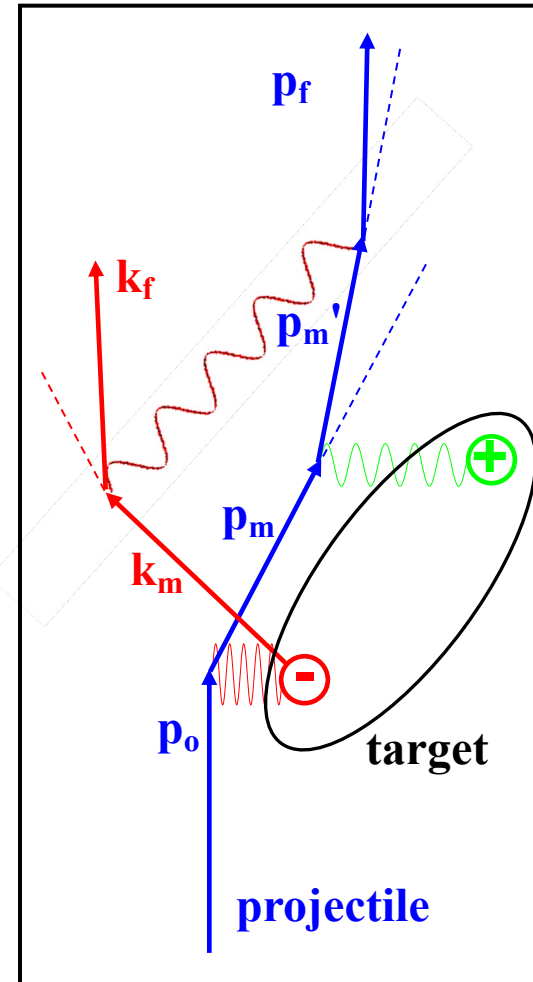
In perturbation theory **understanding few-body dynamics** means describing relative importance of **higher vs first-order** contributions

One important higher-order process: **post-collision interaction (PCI)**

PE – ET – PE
sequence

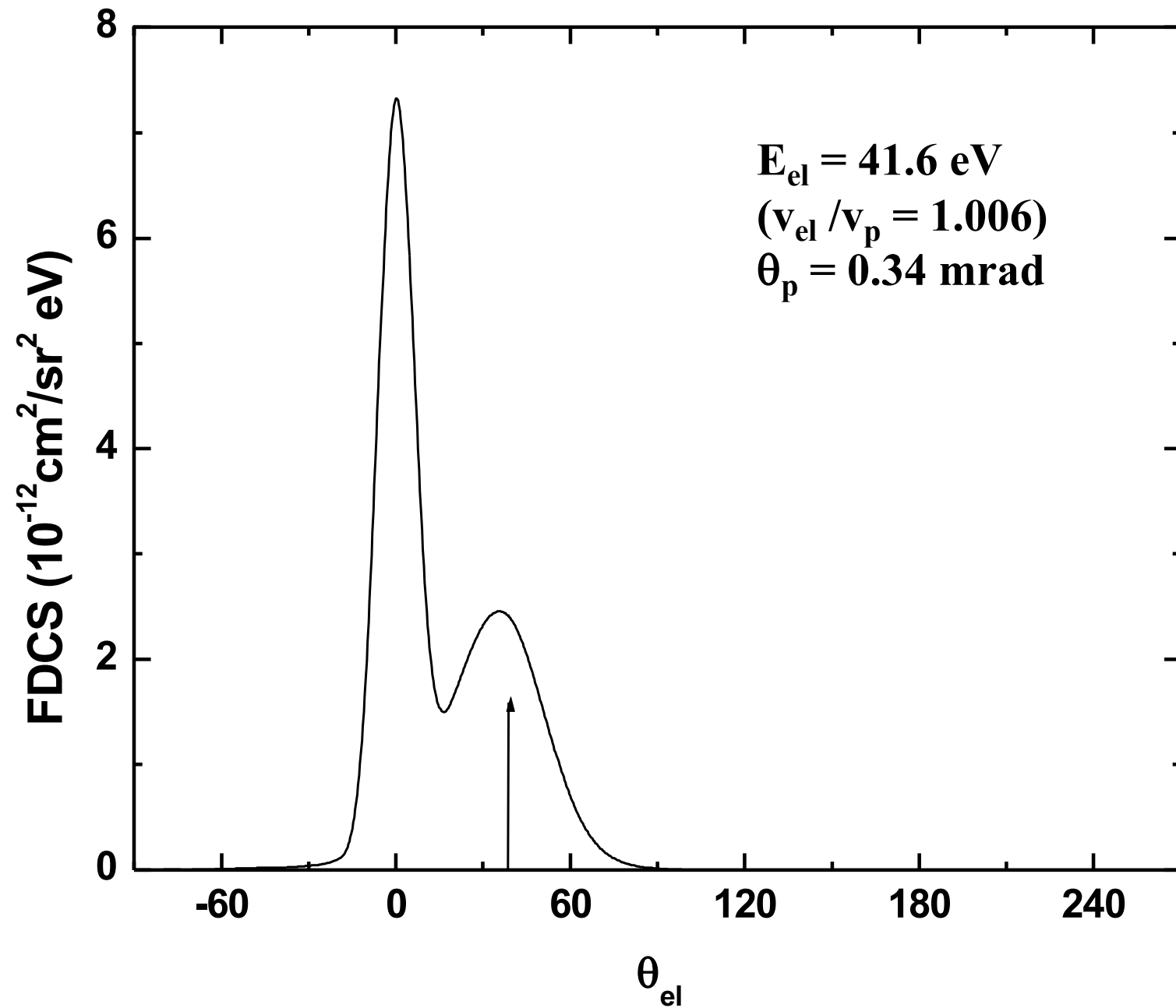


PE – PT – PE
sequence

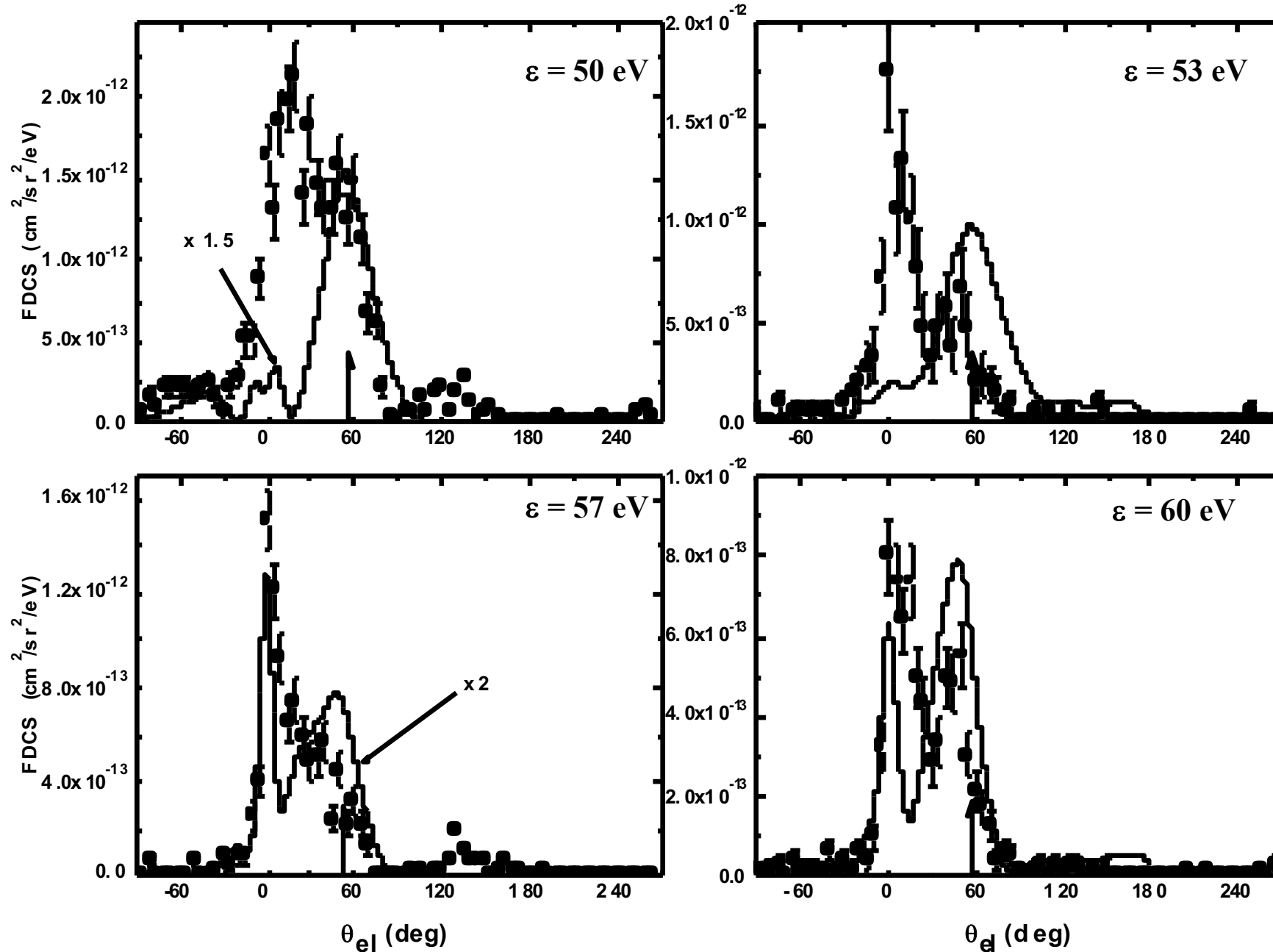


PCI maximizes for $v_{el} = v_p$, for long time **no kinematically complete data available!**

U. Chowdhury et al.,
Phys. Rev. A 83,
032712 (2011)



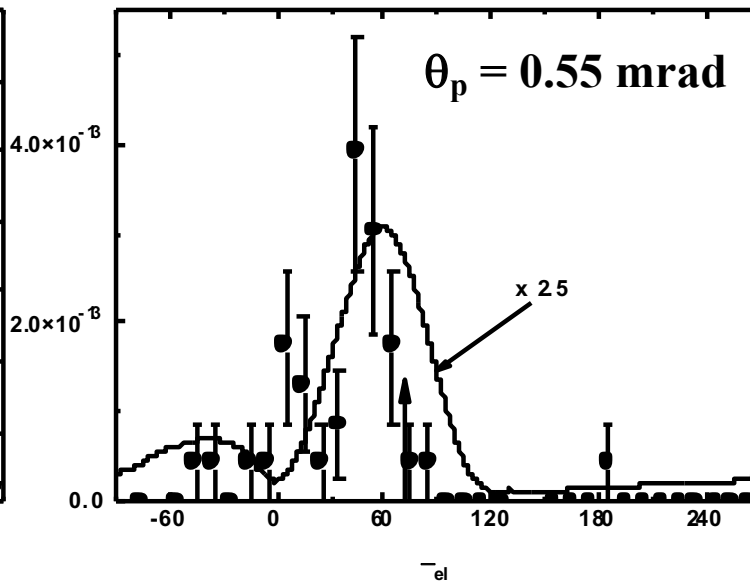
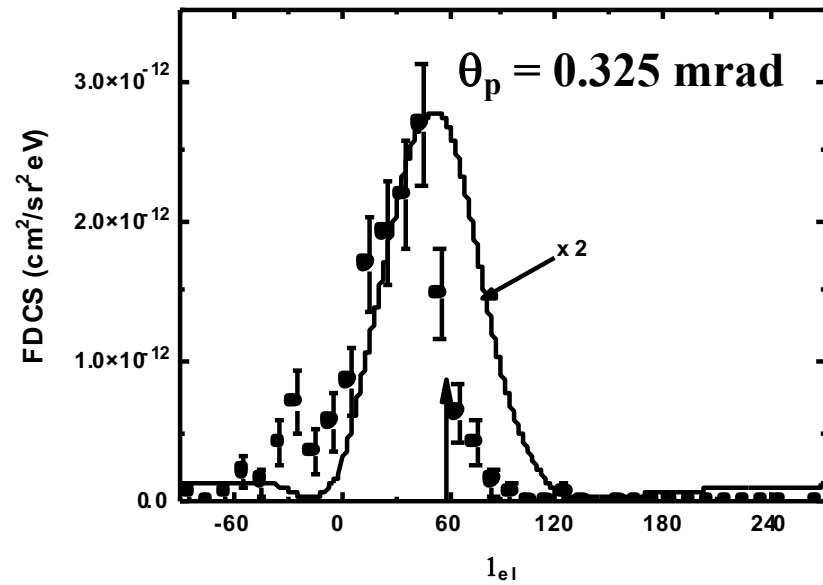
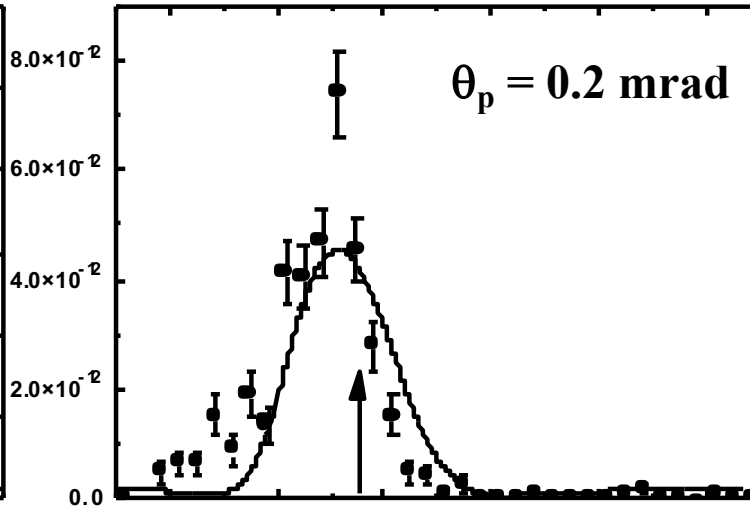
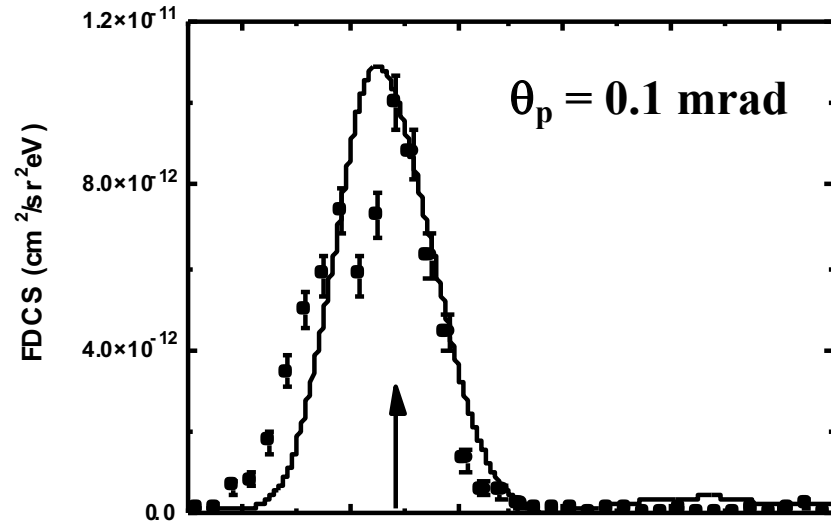
75 keV p + H₂



Electrons
ejected into
scattering
plane
 $\theta_p = 0.55$ mrad

M. Dhital et al.
PRA 99, 062710
(2019)

75 keV p + H₂



Scattering plane
Electron energy = 30 eV

⇒ Discrepancies between experiment and between two **conceptually very similar theoretical models**, which appear to maximize near velocity matching and at large θ_p

⇒ **In these regions FDCS particularly sensitive to details of few-body dynamics!**

Possible causes for discrepancies:

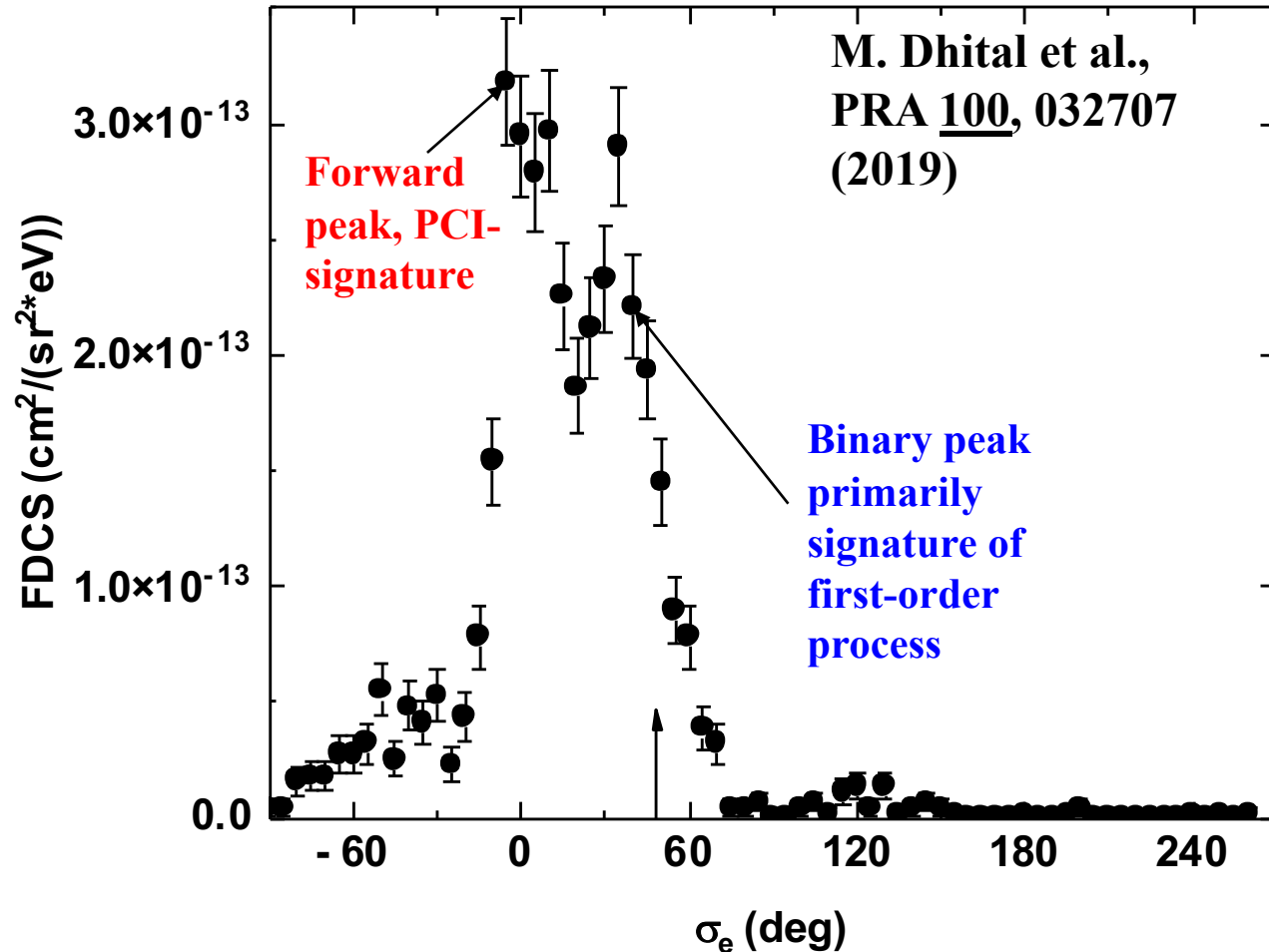
- a) **3C wavefunction inaccurate** if all particles close together.
PE – PT – PE sequence selects such events.

- b) **Capture channel not included** in theory ⇒ due to unitarity capture is erroneously counted as ionization in transition amplitude

Both problems addressed by non-perturbative approaches such as **WP-CCC**. Calculations currently in progress ⇒ **Alisher Kadyrov**

p + He

$\varepsilon = 65.5 \text{ eV}$ ($v_{\text{el}}/v_p = 1$), $\theta_p = 0.5 \text{ mrad}$



2 signatures of PCI:

a) forward peak

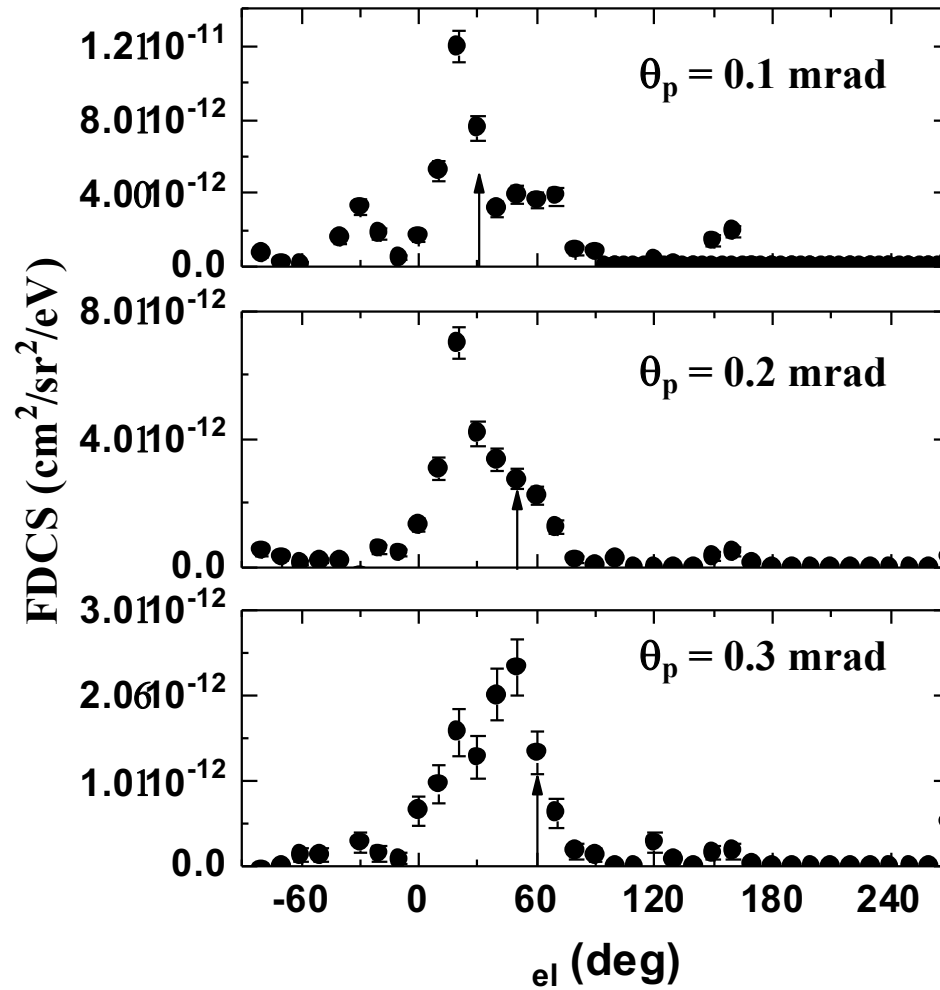
b) forward shift of binary peak

Next project: go as far away as possible from $v_{\text{el}}/v_p = 1$ in order to suppress PCI.

Should enable us to study **non-PCI higher-order effects.**

Use signatures of PCI as monitor for residual PCI contributions

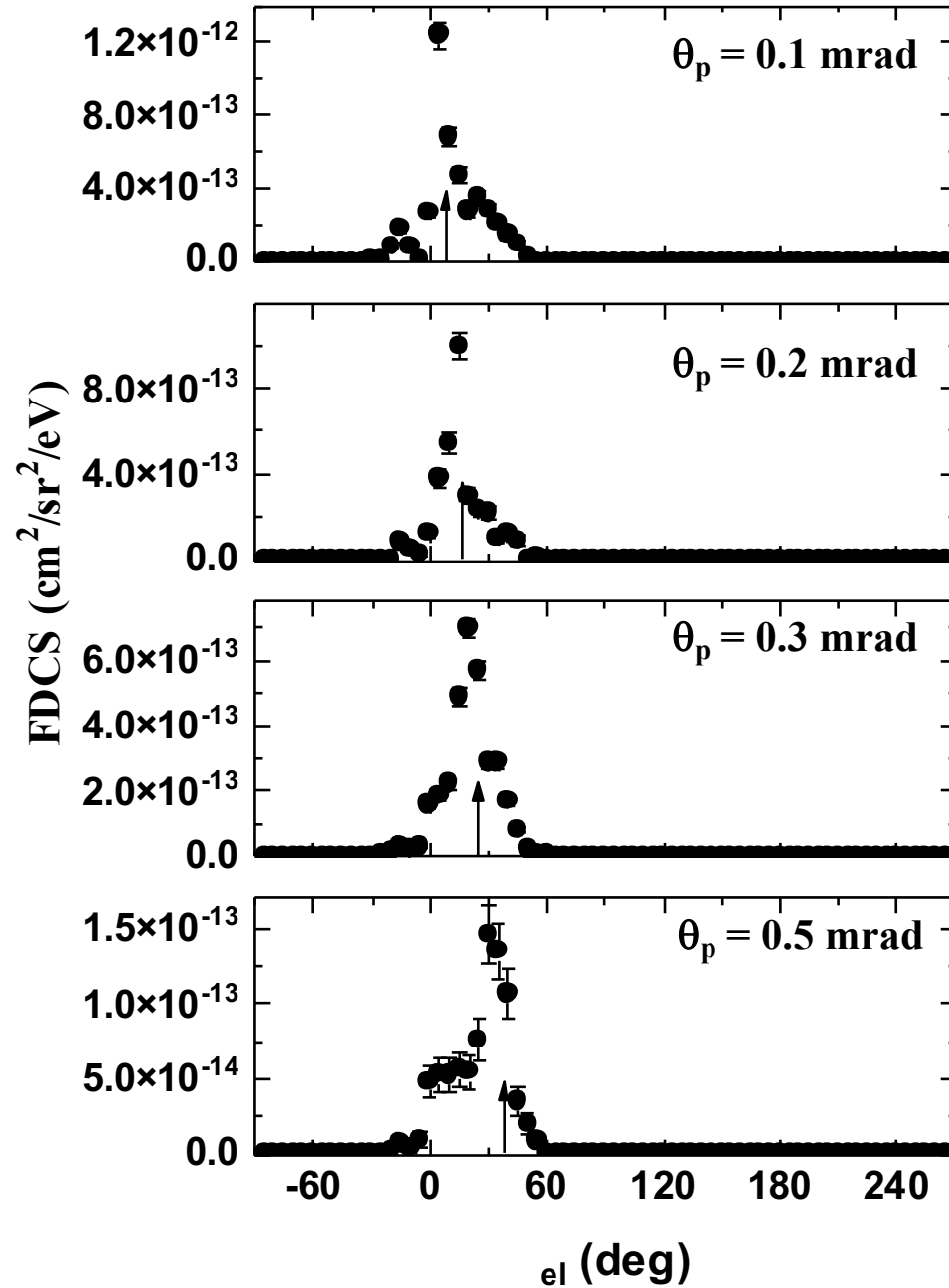
$$\varepsilon = 25.6 \text{ eV}$$



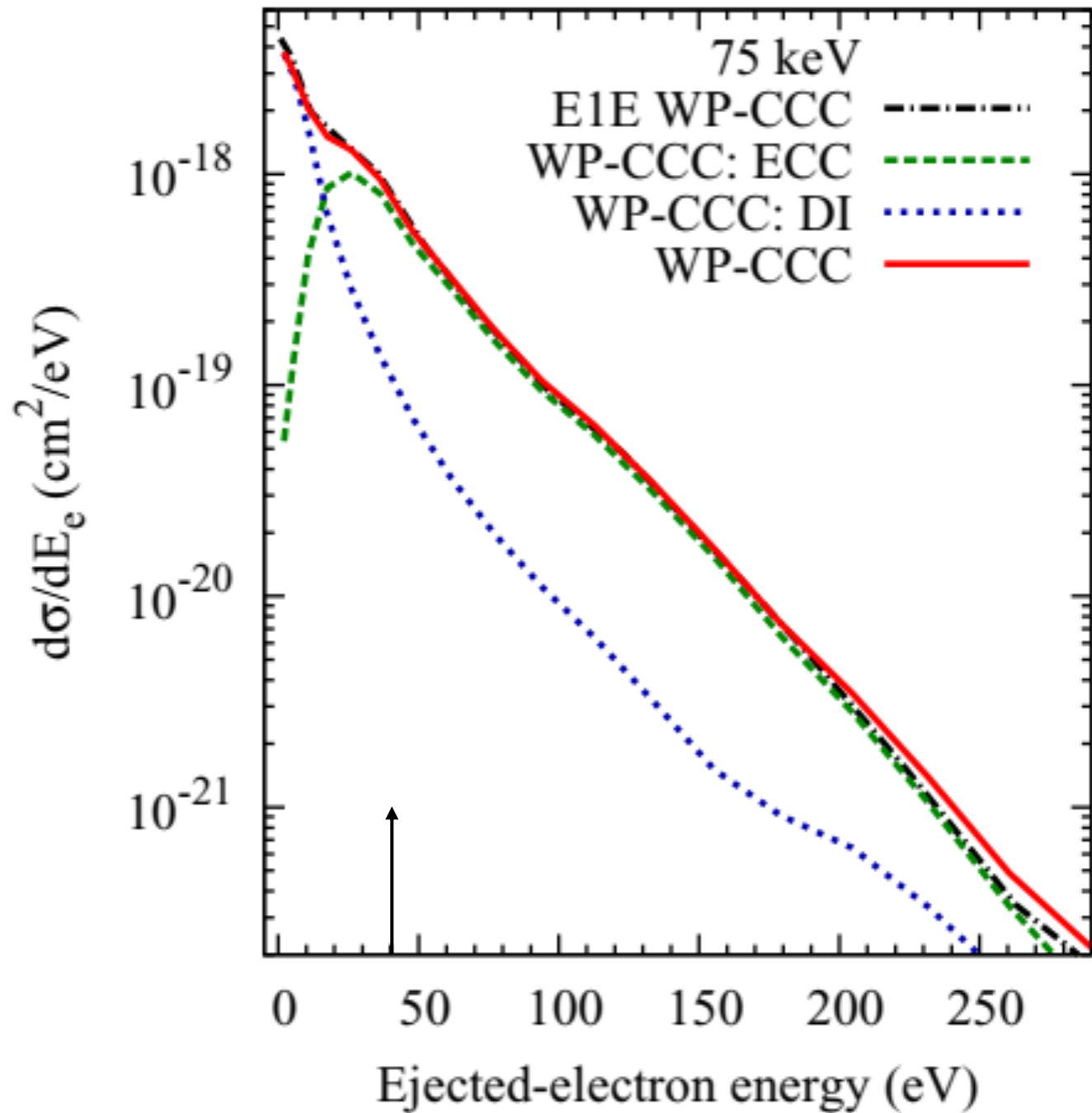
**One PCI signature,
forward peak,
completely absent**

Arrows indicate direction of momentum transfer

$\varepsilon = 100 \text{ eV}$



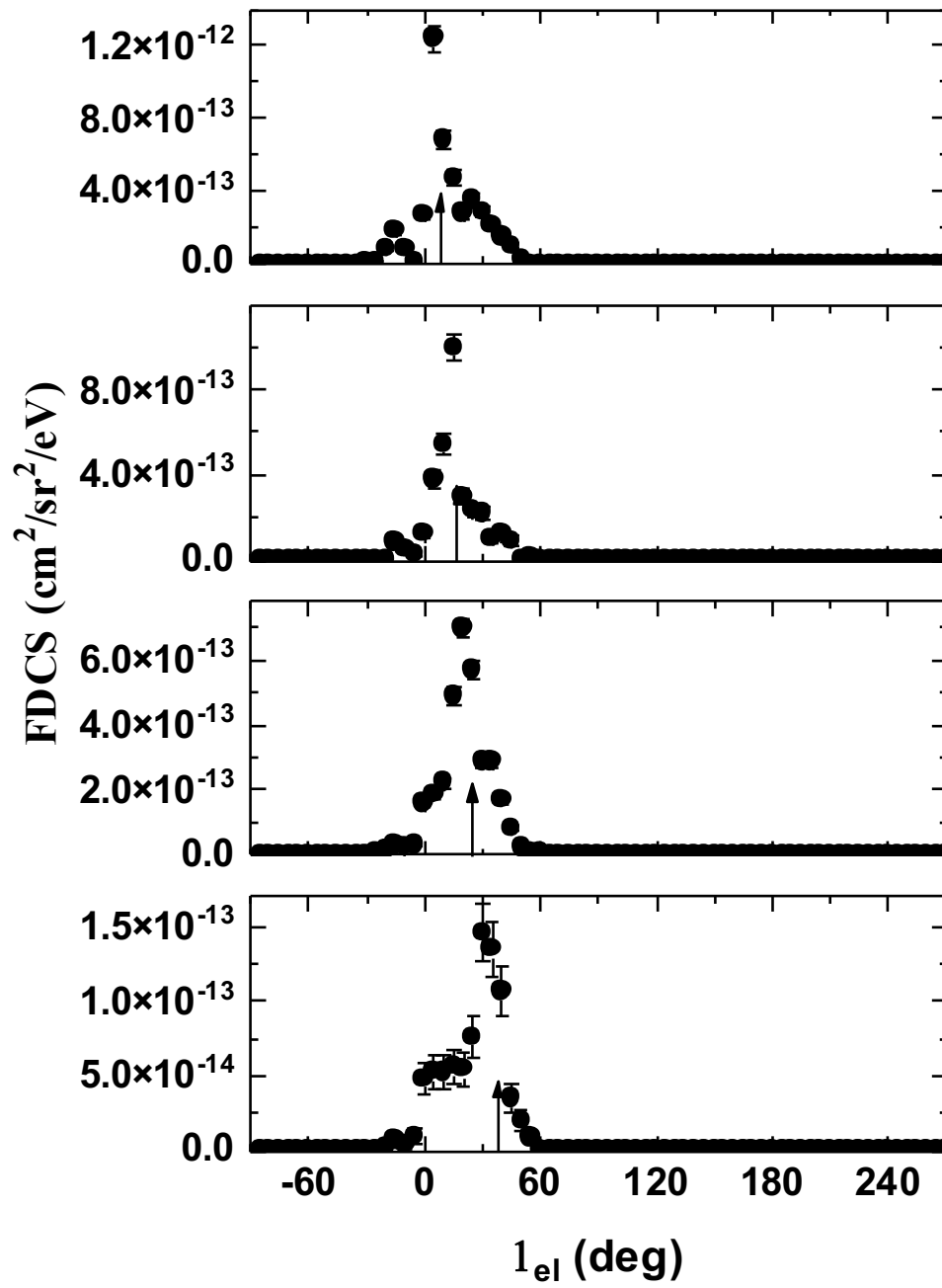
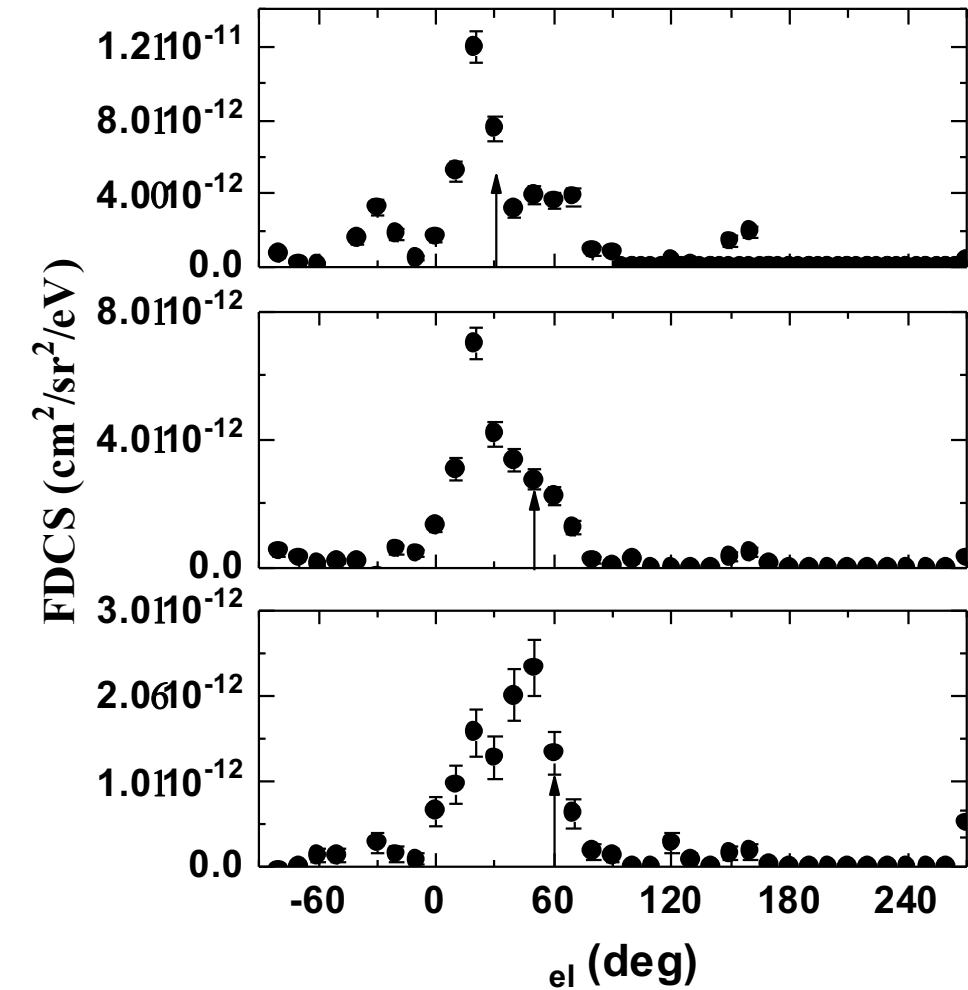
Compared to $v_{el}/v_p = 1$, forward peak strongly suppressed, but compared to $v_{el}/v_p \ll 1$ a significant residue remains



**K.H. Spicer et al.,
PRA 104, 052815
(2021)**

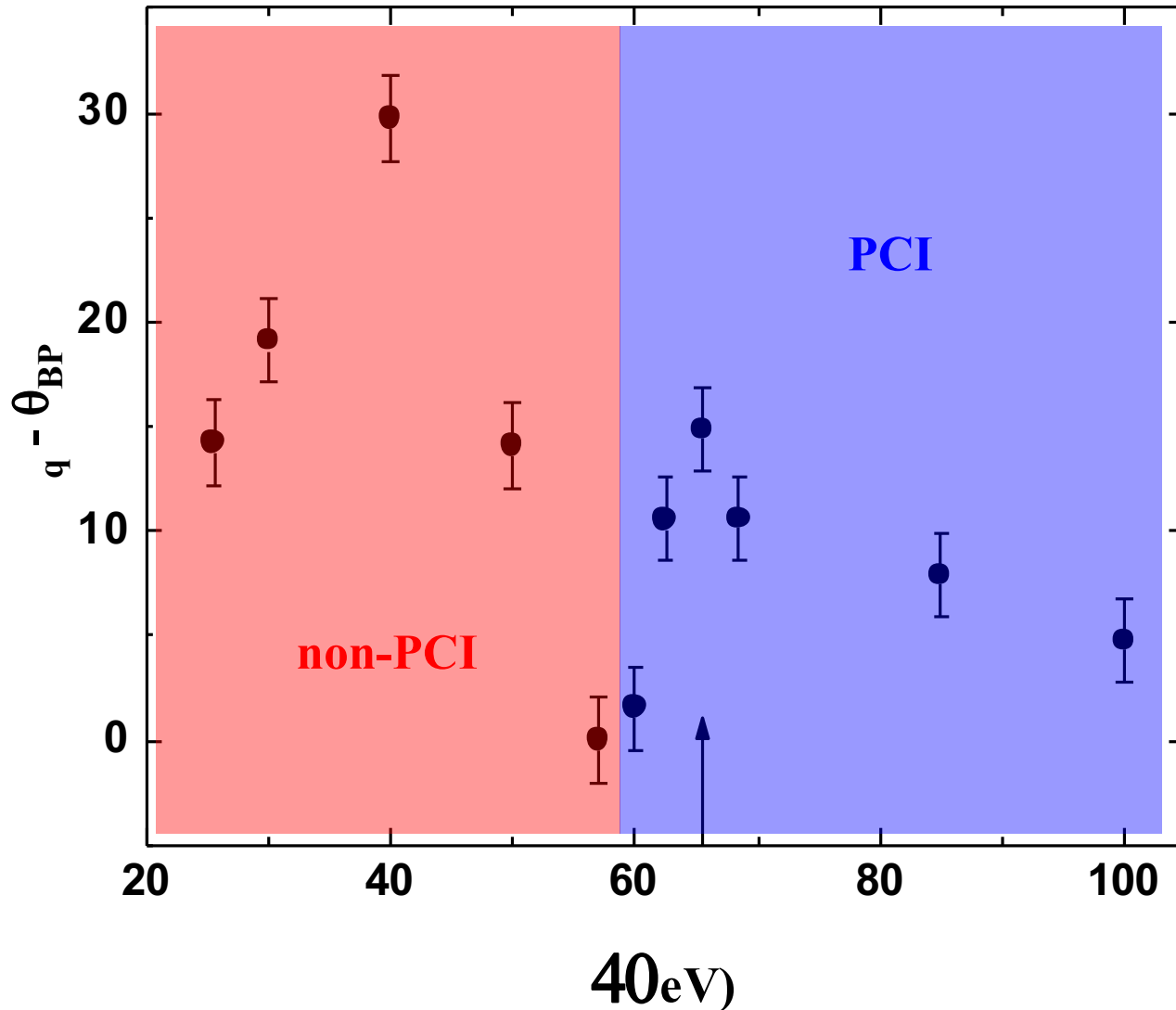
$\varepsilon = 25.6 \text{ eV}$

$\varepsilon = 100 \text{ eV}$



Forward shift is
larger at
 $\varepsilon = 25.6 \text{ eV}$,
BUT ...

... Schulz et al. PRA 88, 022704 (2013): projectile – target nucleus interaction can also lead to forward shift



2 components to forward shift, one contributes only at $v_{el}/v_p < 1$, the other only **near and above** $v_{el}/v_p = 1$.

Forward shift for $\epsilon = 100$ eV caused **mostly by PCI**, but for $\epsilon = 25.6$ eV **mostly due to non-PCI effects?**

Conclusions

- **FDCS for ionization measured for a broad range of electron energies**
- **Near velocity matching PCI signatures: a) forward peak b) forward shift of binary peak**
- **Forward peak absent far below, but residue remains far above matching velocity**
- **Not every forward shift of binary peak is signature of PCI**
 - **far below matching velocity non PCI higher-order effects**
 - **above matching velocity mostly due to PCI**
- **Without **Don Madison** and his distorted wave calculations we would not be where we are. But now non-perturbative calculations needed.**